

# News on continuous variables

Contributions from Potsdam node to the goals of **COMPAS**

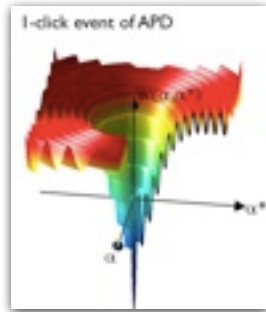
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**Matthias Ohliger and Jens Eisert**  
University of Potsdam, Germany



Partly joint work with Konrad Kieling and Andrea Mari  
Brussels, December 2009

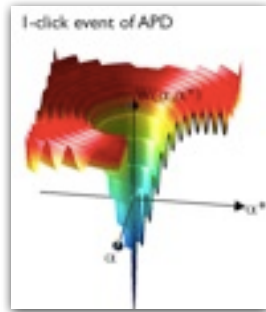
## • Overview:



## • Systems identification and detector tomography

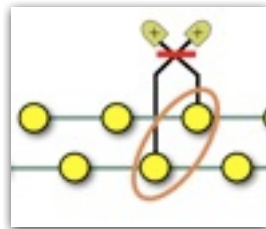
- "Learn much from little": Ideas of *systems identification* with error bars
- *Detector tomography*
- Measures of *non-classicality* (negative Wigner functions) and how to measure them
- Entanglement in *multi-mode states*
- Applications to *CV entanglement distillation*

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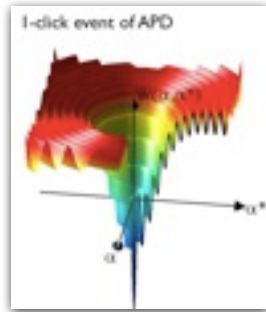
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## • Quantum computation with non-Gaussian states

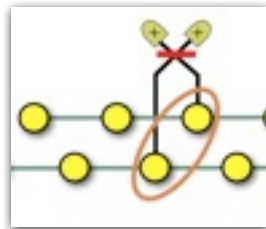
- *No-go statements* on Gaussian approaches to measurement-based quantum computing
- Full potential of *non-Gaussian states for computing*

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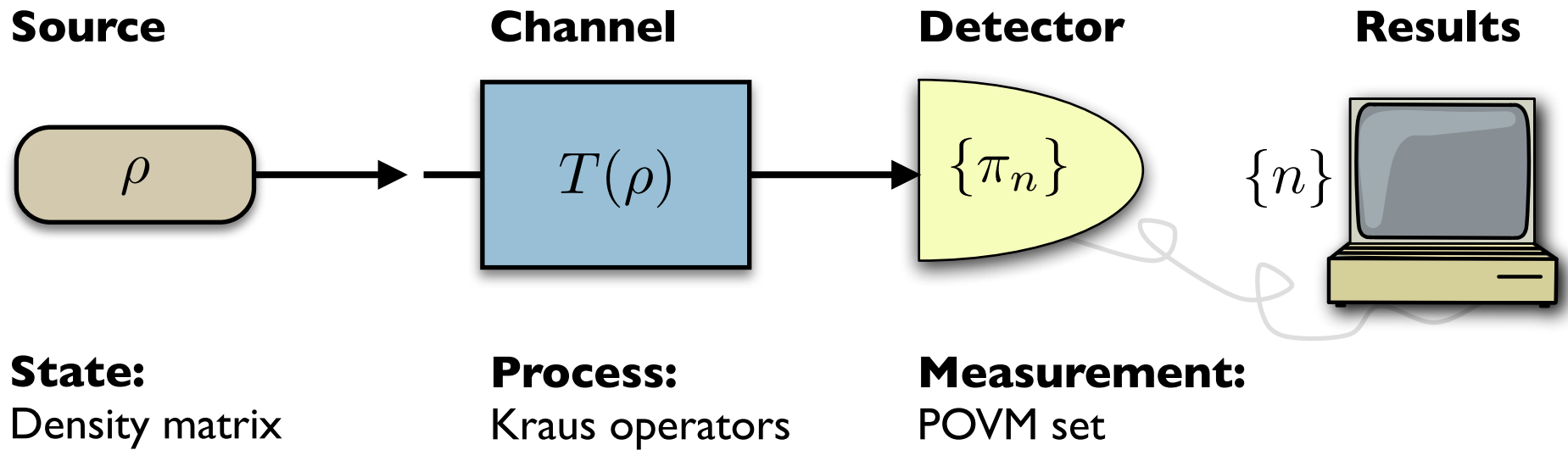
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- Full potential of *non-Gaussian states for computing*



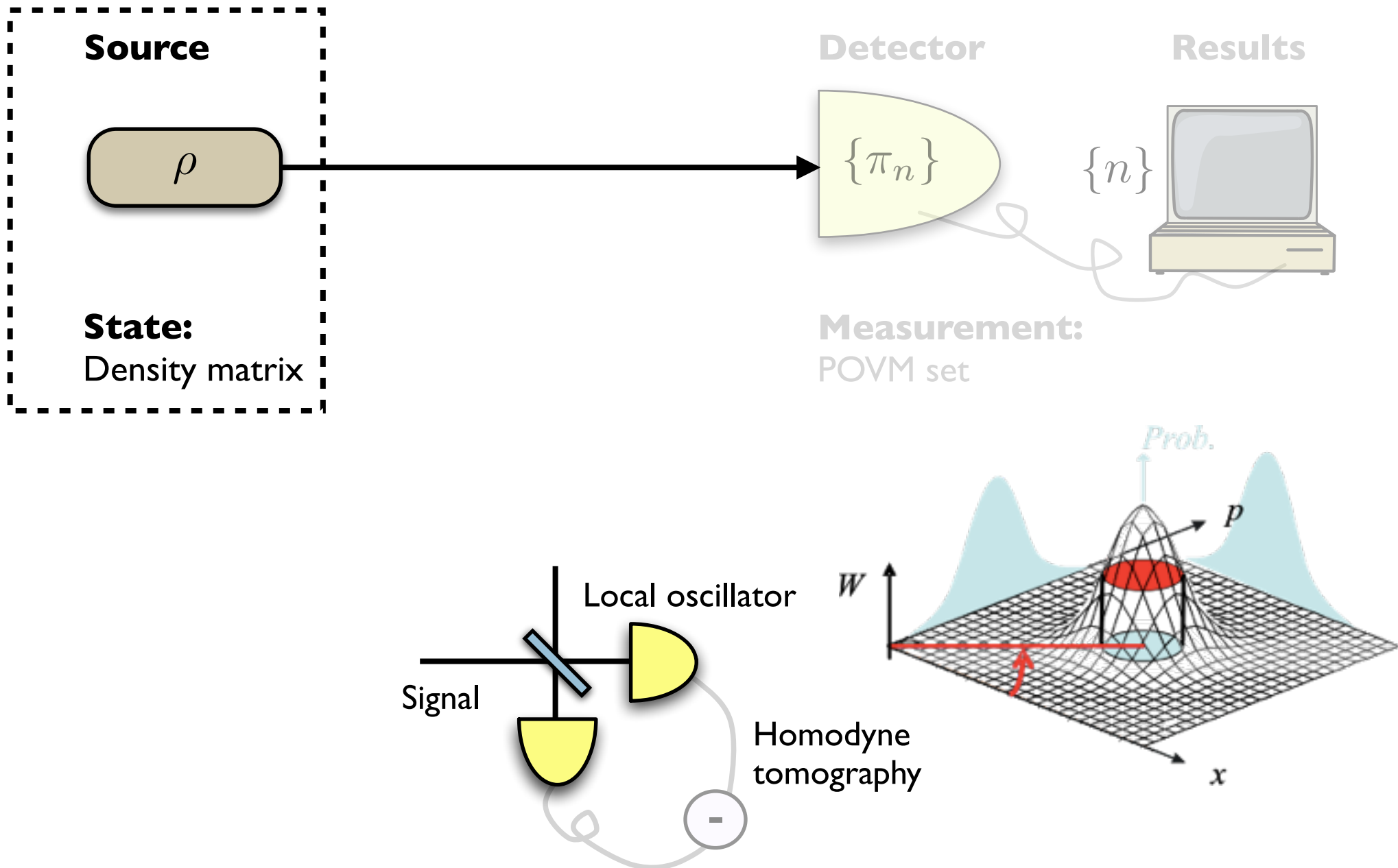
## • Some perspectives

- **Detector tomography and certifiable bounds for CV entanglement and non-classicality**

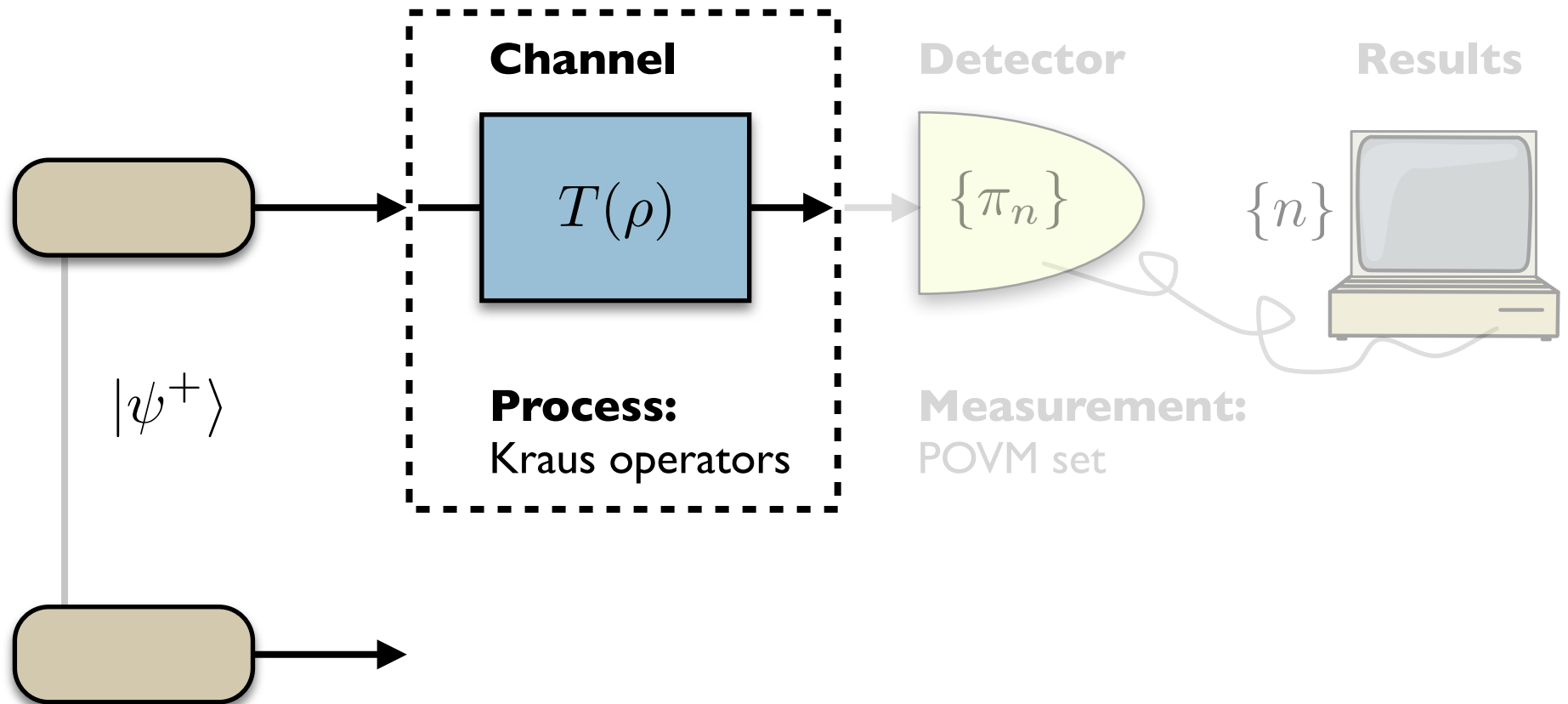
## • A typical quantum experiment



# • State tomography



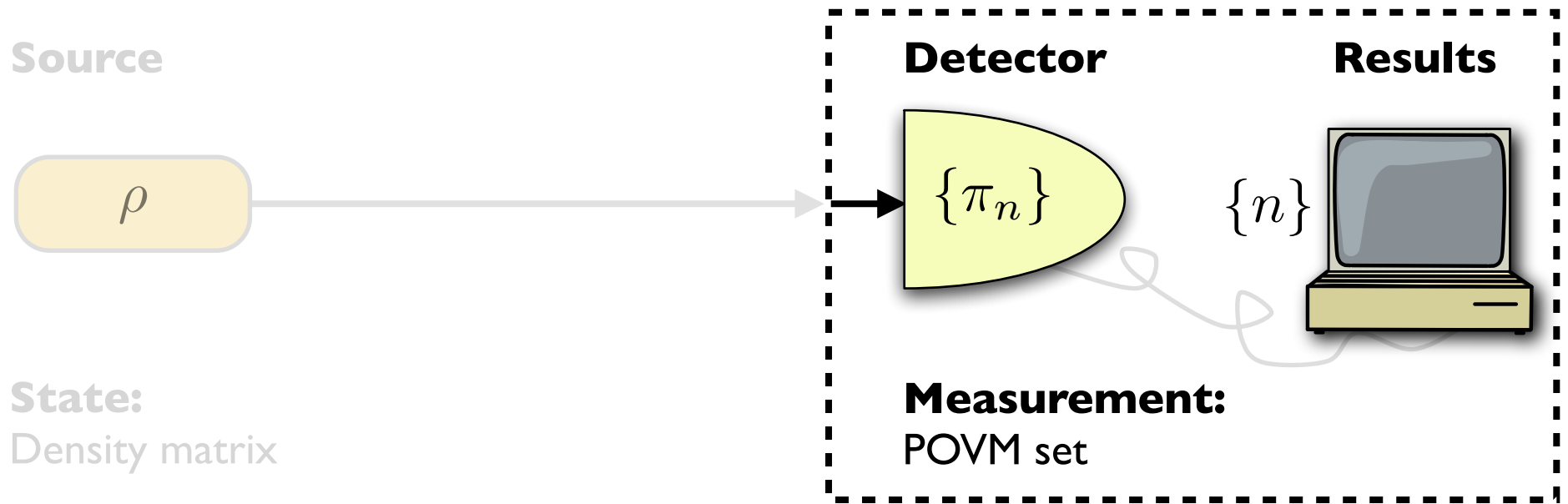
## • Process tomography



- State tomography on channel acting on entangled input



## • Completing the triangle: Detector tomography



- Positive operator valued measure (**POVM**) of detector

$$\begin{aligned} \sum_K \pi_n &\geq 0 && \text{(One POVM element per outcome)} \\ \sum_{j=1} \pi_j &= \mathbb{I} && \text{(Completeness)} \end{aligned}$$

- **Reconstruction:**

$$p_n(\rho) = \text{tr}(\rho\pi_n)$$

Need to know **results** and **states** to get **POVM** elements (tomographically complete probe set)

## • **Completing the triangle: Detector tomography**

- Calibration of detectors difficult, therefore employ „Black Box Approach“
- Sending coherent states to the detector measures Q-Function

$$Q(\alpha, \alpha^*) = \langle \alpha | \rho | \alpha \rangle$$

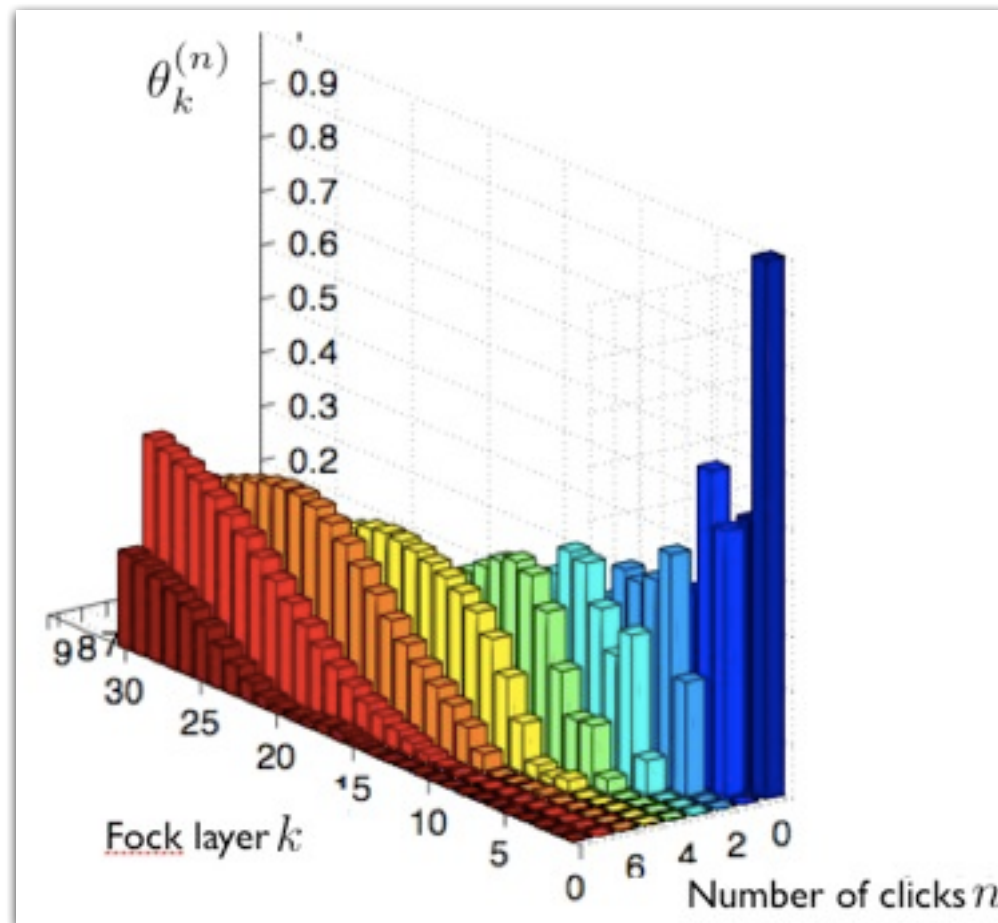
- Due to noise, Q-Function can correspond to non-physical POVM-element
- When no phase dependence observed:  $\pi_n = \sum_{k=0}^{\infty} \theta_n^k |k\rangle \langle k|$
- Find physical POVM closed to the one corresponding to the measured statistics

$$P = F\Pi \quad F_{i,k} = \frac{|\alpha_i|^{2k} \exp(-|\alpha_i|^2)}{k!}$$

$$\min \{ \|P - F\Pi\|_2 + g(\Pi) \}$$

$$\text{subject to} \quad \sum_{n=1}^N \pi_n = 1 \quad \pi_n \geq 0$$

- **Completing the triangle: Detector tomography**



## • **Detecting negative Wigner functions**

- Negative Wigner function is a sign of non-classicality.
- Pure state: Wigner function positive if and only if the state is Gaussian
- Mixed states: State with positive Wigner function can be „a little“ non-Gaussians e.g. mixtures of Gaussian states.
- Quantitative Measure:

$$N = \int |W(\xi)| d\xi - 1$$

## **Bound from „few“ measurements**

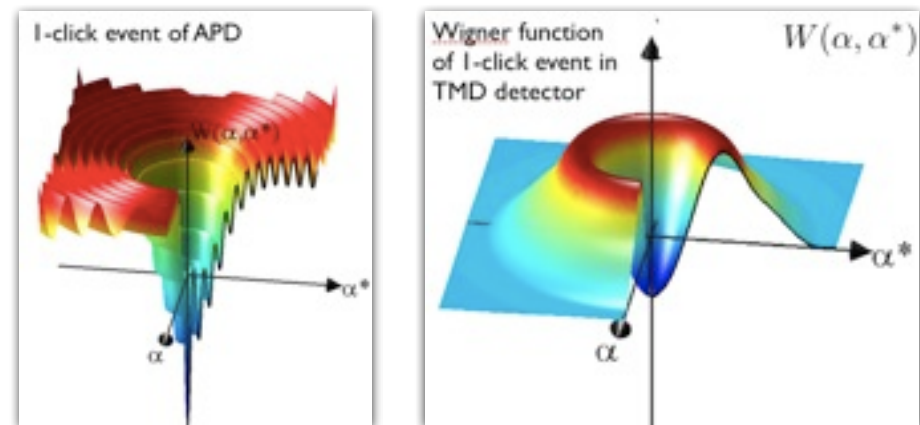
- Find the state with the *lowest* Wigner-functions-negativity consistent with given measurement statistics

## • Projects in last period:

### I. Experimental implementation/theoretical analysis of detector tomography

#### DI.6

- Including techniques of filtering in ill-conditioned settings
- Applications to weak homodyning: Photon counting with a weak phase reference as a "hybrid" between a CV and a discrete variable approach

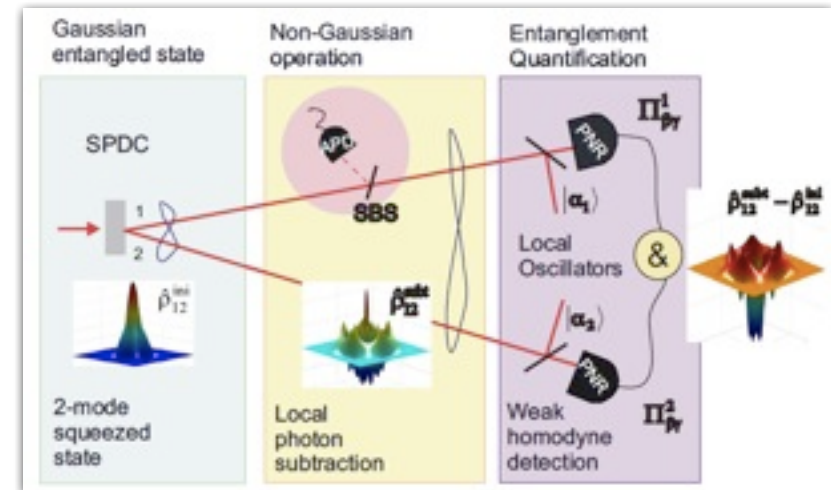


- *Measuring measurement: theory and practice*, A. Feito, J. Lundeen, H. Coldenstrodt-Runge, J. Eisert, M.B. Plenio, and I.A. Walmsley, *New Journal of Physics* **11**, 093038 (2009)
- *A proposed testbed for detector tomography*, H.B. Coldenstrodt-Runge, J.S. Lundeen, K.L. Pregnell, A. Feito, B.J. Smith, W. Maurer, C. Silberhorn, J. Eisert, M.B. Plenio, I.A. Walmsley, *Journal of Modern Optics* **56**, 432 (2009)
- *Tomography of quantum detectors*, J. Lundeen, A. Feito, H. Coldenstrodt-Runge, T.C. Ralph, C. Silberhorn, J. Eisert, M.B. Plenio, and I.A. Walmsley, *Nature Physics* **5**, 27 (2009)

## • Projects in last period:

### 2. Good direct bounds to entanglement

- Bounds from few measurements of a weak homodyning measurement:
- "Minimal degree of entanglement consistent with measurements", based on much less than tomographic knowledge
- Tool to certify success of CV entanglement distillation



- Entanglement quantification from incomplete measurements: Applications using photon-number-resolving weak homodyne detectors, G. Puentes, A. Feito, A. Datta, J. Eisert, M.B. Plenio, I.A. Walmsley, arxiv.org:0911.2482

### 3. Directly detecting negative Wigner functions

- Direct bounds with error bars from mere two slices in phase space
- Including certified bounds to a *non-classicality measure* based on the negativity of the Wigner function
- Tight practical bounds for photon subtraction
- Connection to non-Gaussianity measures

- Directly detecting negative Wigner functions, A. Mari, K. Kieling, J. Eisert, in preparation (2009)

### 4. Characterization of spatially entangled photon pairs

- Two-dimensional characterization of spatially entangled photon pairs, M. Ostermeyer, D. Korn, P. Pihlmann, C. Henkel, and J. Eisert., Journal of Modern Optics, iFirst November (2009).

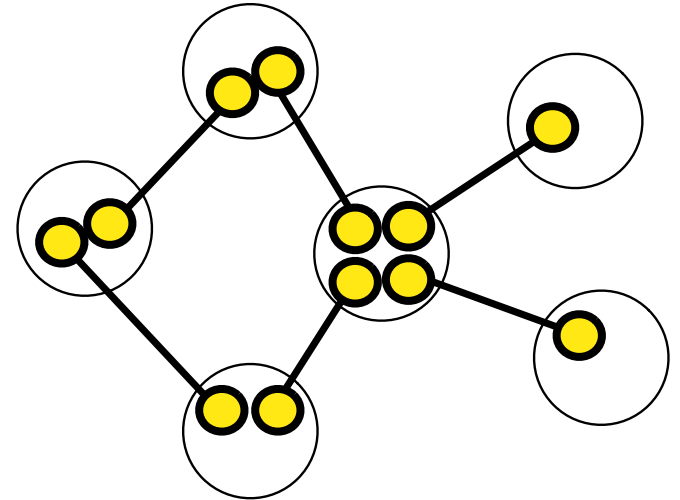
DI.I

- **Measurement based quantum computing with CV-quantum states**



## • Realistic Gaussian Cluster states:

- Start every mode in finitely squeezed vacuum state and employ Gaussian operation between „neighboring“ pairs
- Generalization to Gaussian Projected Entangled Pair States (GPEPS)



## • Resource for Measurement Based Quantum Computing ?

- For Gaussian measurements, no entanglement between distant points:

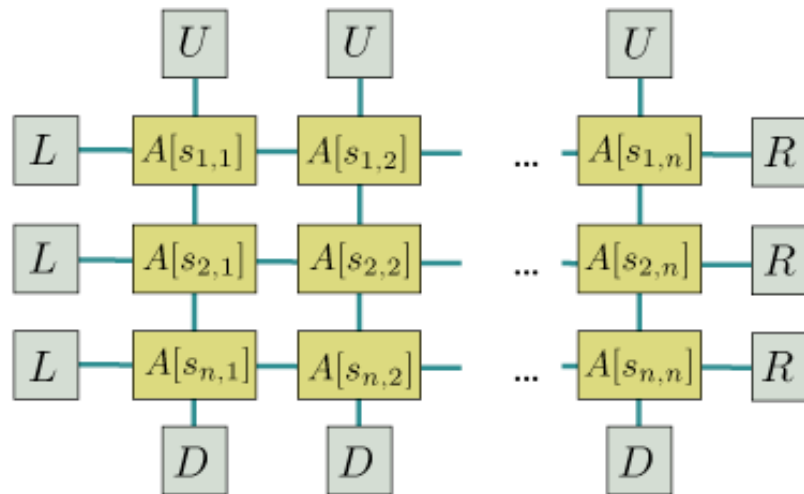
$$E_G(A, B) \leq C e^{-d(A, B)/\xi}.$$

- Strong connection to Gaussian repeater networks for entanglement distribution



## • **Non-Gaussian CV-resource states for MBQC:**

- CV computational tensor network states with *finite-dimensional* correlation system



- Efficiently describable but not efficiently simulatable
- Restricted set of measurements based on physical feasibility, e.g. homodyning, single-photon detection
- Allow for computing with homodyning only (on the expense of difficult resource state)

# • Non-Gaussian CV-resource states:

Sequential interaction with two-dimensional ancilla system with particular class of Hamiltonians

-Schoen, Hammerer, Wolf, et. al, *Phys Rev A* **75** (2007)

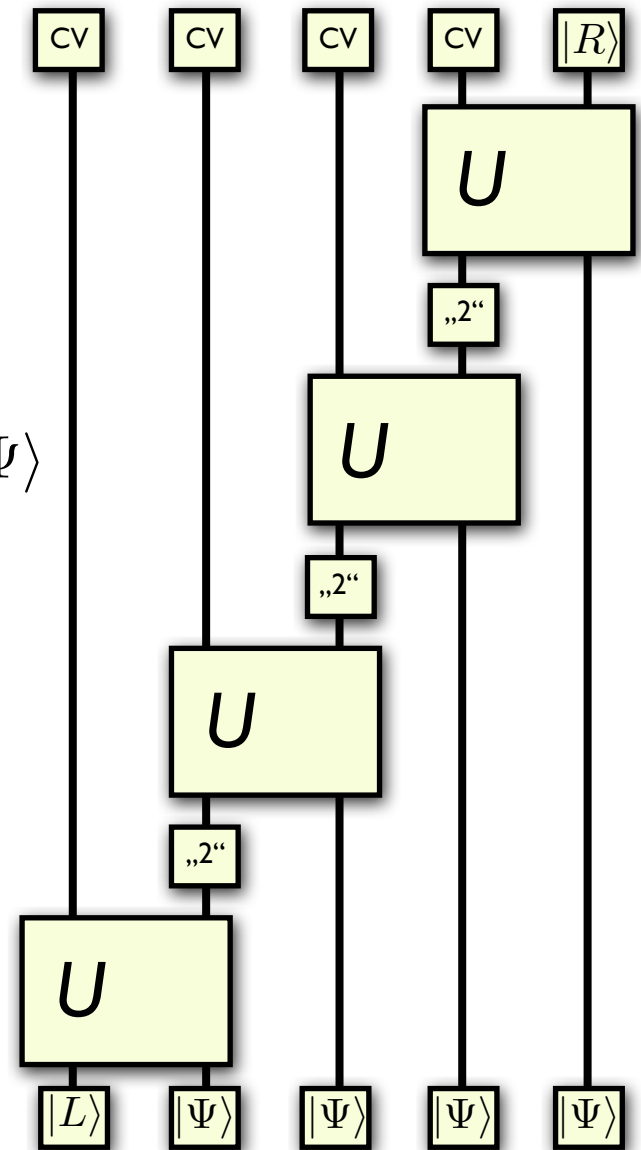
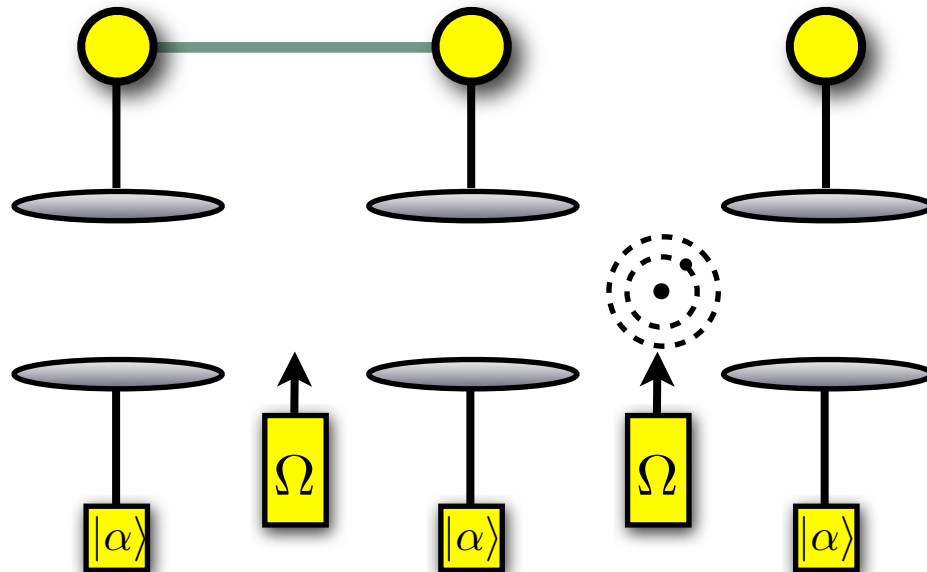
$$H = \sum_{s=0}^{\infty} H_2(s) \otimes |s\rangle\langle s|$$

Hamiltonian on qubit subspace

$$U(s) = e^{-iH_2(s)t}$$

Fock basis of light mode

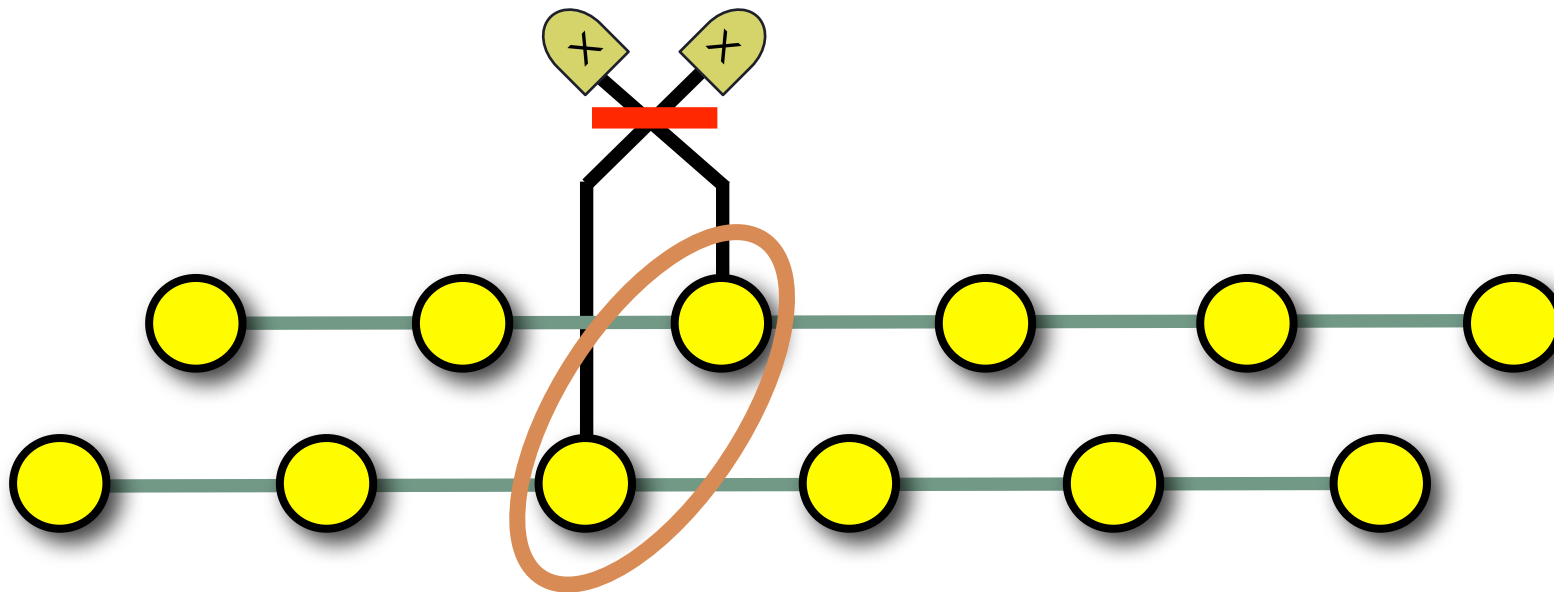
$$A[\phi] = \sum_{s=0}^{\infty} U(s) \langle \phi | s \rangle \langle s | \Psi \rangle$$



$$U = e^{-iHt}$$

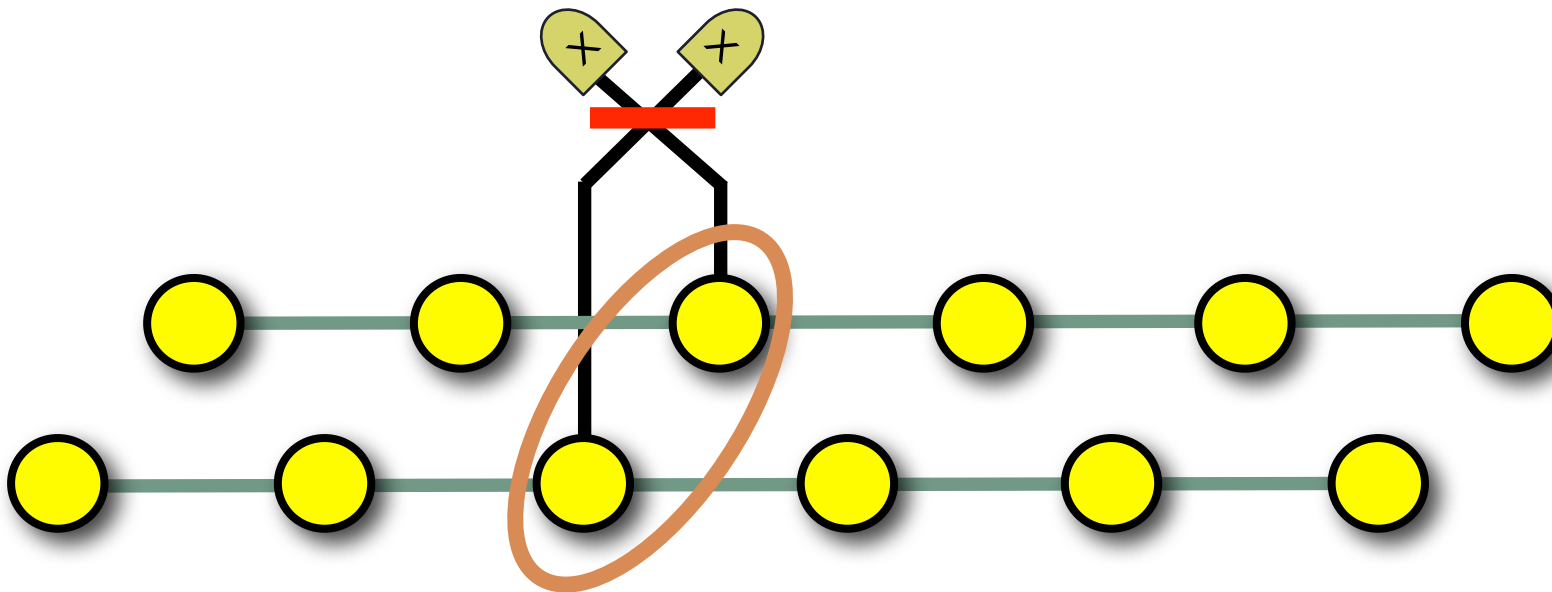
- **Non-Gaussian CV-resource states:**

- Coupling of two logical wires by “simple” joined measurements



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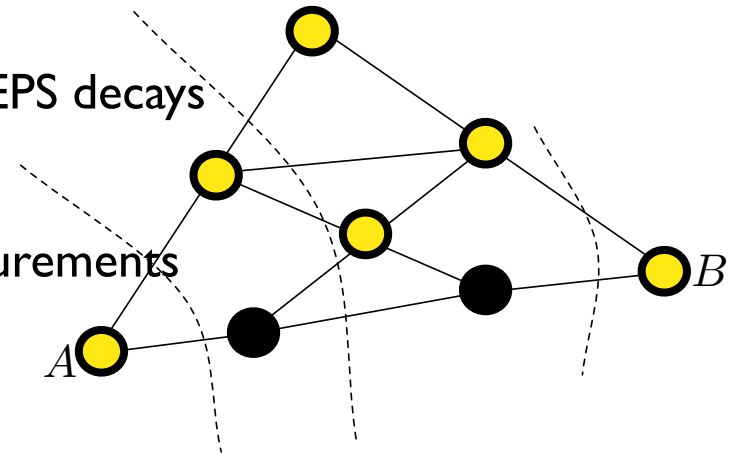
- **Important questions:**

- How to handle inherent randomness?
- How to perform error correction?

## • Projects in last period:

### 5. Limitations of Gaussian cluster state computing

- Gaussian *localizable entanglement* between two points in a GEPS decays exponentially with the distance between them
- For one-dimensional GPEPS even true under arbitrary measurements
- Percolation strategies on general graphs
- *Limitations of quantum computing with Gaussian cluster states*, M. Ohliger, K. Kieling, J. Eisert, to be published

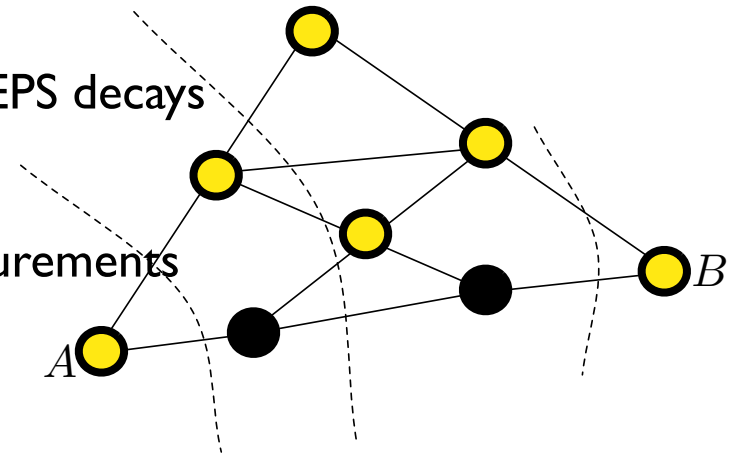


**DI.2/D2.5**

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**DI.2/D2.5**

### 6. MBQC with non-Gaussian resources

- General classification of one-dimensional CV-resources  
(Extension of *Quantum computational webs*, D. Gross, J. Eisert, arXiv: 0810.2542)
- Efficient measurement scheme by homodyne detection only
- Resource preparation by Jaynes-Cummings type interaction
- M. Ohliger, K. Kieling, J. Eisert, to be published

**DI.2**

- **Some perspectives**

- **Think more in terms of CV-discrete hybrid approaches:**

- Photon counting with weak phase reference (weak homodyning), quantum dot sources ...
- ... aiming at exploiting advantages of "both worlds"

- **More on computing:**

- Explore full potential of non-Gaussian states for QC
- Small-scale computing, say, in quantum repeaters

- **More on physical hybrids:**

- Link results of last years on CV quantum information more to hybrid architectures, combining CV light with cold atoms

- **Combining CV-light with optomechanics:**

- Transferring non-classicality between CV light and optomechanical systems

- **More on entanglement purification and distillation:**

- Realize fully-fledged entanglement distillation



- **Systems identification:**

- Compressed sensing paradigm to measuring quantum objects
- Emphasize paradigm of having error bars

- **Metrology:**

- Explore full potential of non-Gaussian states for metrology applications

- Thanks!